

# PHYS405 - Advanced Computational Physics

## Assignment #8

Due: Friday, November 20

*Purpose:* Learn how to solve PDEs using parallel computers.

*Note:* Please identify all your work.

### Solving Poisson Equation

You are to solve Poisson equation in a parallel code. This elliptic PDE is typically used in demonstrating how to numerically solve PDEs. It has the advantage of being time independent. In 2D, it takes the form of

$$\frac{\partial u(x, y)}{\partial x^2} + \frac{\partial u(x, y)}{\partial y^2} = S(x, y) \quad (1)$$

where the field  $u(x, y)$  is solved for in a domain in  $x$  and  $y$  with specified boundary conditions and source term  $S(x, y)$ .

### Steps

- Use finite difference approach on an equally spaced square lattice to solve the PDE.
- Start with the serial 2D Poisson solver code ( *poisson\_2d.c* ) in the course web pages. Use the physical set-up as in this code, namely use the domain, the gaussian source, and the Dirichlet boundary conditions as specified in this code.
- Parallelize the code.
- Use the parallel *Game of Life* (*parallel\_life\_game.c*) and the 1D Poisson equation solver (*poisson\_parallel\_1d.c*) codes as guides.
- Use MPE or a pipe in the Python graphic code (*plot\_image.py*) to display the solution.
- Compare your solution (map image of  $u(x, y)$ ) to the serial code solution as a rough check of the code.
- Replace the solution back in the Poisson equation as a further (MORE PRECISE) check of the solution (as is done in the serial code).
- Make sure your code works for arbitrary lattice size and number of processors.